This is the code to generate the data presented in Figure 3 of the the paper "Induction with and without natural properties: a new approach to the New Räddle of Induction". "The program was created in Visual Studio 2019. "To run the program, create a windows form application with single button "Button I", paste this code into FormI.vb, and place a breakpoint at line 502 (End Sub). "After executing the program, press Button 1. Sample_Size is currently set to 8. In order to generate the data for Figure 3, you will need to run the program 6 times for the 6 sample sizes presented in the figure. "Once the program breaks at line 509, data of the type presented in Figure 3 will have been outputted to an Excel file. Imports System.Math

Public Class Form1

Dim Big_Loop_Size AS Integer = 1000 Dim Number_of_Objects As Integer = 1000000 Dim Sample_Size AS Double = 8 Dim Number_of_Dimensions AS Integer = 4 Dim Number_of_Natural_Categories AS Double = 8 Dim Std_Dev_for_Natural_Categories AS Double = 0.2 Dim Number_of_Centroids AS Integer = 8 'Number_of_Natural_Categories

Dim Natural_Category_Means(Number_of_Natural_Categories, Number_of_Dimensions) As Double Dim Natural_Category_Probabilities(Number_of_Natural_Categories) As Double

Dim Natural_Category_Counts(Number_of_Natural_Categories) As Double

Dim Object_Coordinates(Number_of_Objects, Number_of_Dimensions) As Double

Dim Centroid_Coordinates(Number_of_Centroids, Number_of_Dimensions) As Double Dim Provisional_Centroid_Coordinates(Number_of_Centroids, Number_of Dimensions) As Double Dim Top_Centroid_Coordinates(Number_of_Centroids, Number_of Dimensions) As Double

Dim Distance_Holder1 As Double Dim Distance_Holder2 As Double

Dim Object_Centroid_Assigment(Number_of_Objects) As Double Dim Object_Provisional_Centroid_Assigment(Number_of_Objects) As Double Dim Object_Updated_Centroid_Assigment(Number_of_Objects) As Double Dim Object_Top_Centroid_Assigment(Number_of_Objects) As Double

Dim Updated_Centroid_Coordinates(Number_of_Centroids, Number_of_Dimensions) As Double

Dim Total_Object_to_Assigned_Top_Centroids_Distance As Double Dim Total_Object_to_Assigned_Provisional_Centroids_Distance As Double Dim Total_Object_to_Assigned_Updated_Centroids_Distance As Double

Dim Number_of_Objects_Attached_to_Centroid_Counter As Double

Dim objectcounter As Integer

Dim Sample_Object_Coordinates(Sample_Size, Number_of_Dimensions) As Double
Dim Sample_Object_Top_Centroid_Assigment(Number_of_Objects) As Double

Dim Object_to_Fitted_Category_Count(Number_of_Centroids) As Double Dim Object_to_Fitted_Category_in_Sample_Count(Number_of_Centroids) As Double

Dim Mean_Distance_from_frequencies_in_Universe_and_Sample_for_fitted_Classes As Double

Dim Fitted (lass Frequencies_in_Sample(Number_of_Centroids) As Double Dim Fitted (lass Frequencies_in_Universe(Number_of_Centroids) As Double Dim Rectangular_Category_Frequencies_in_Sample(Number_of_Centroids) As Double Dim Rectangular_Category_Frequencies_in_Universe(Number_of_Centroids) As Double Dim Non_convex_Category_Frequencies_in_Universe(Number_of_Centroids) As Double Dim Non_convex_Category_Frequencies_in_Universe(Number_of_Centroids) As Double Dim Non_convex_Category_Frequencies_in_Universe(Number_of_Centroids) As Double

Dim Fitted_Category_Accuracy(Big_Loop_Size) As Double Dim Rectangular_Category_Accuracy(Big_Loop_Size) As Double 'Dim Non_convex_Category_Accuracy(Big_Loop_Size) As Double

Dim Mean_Fitted_Category_Accuracy As Double Dim Mean_Rectangular_Category_Accuracy As Double 'Dim Mean_Non_convex_Category_Accuracy As Double

Dim RandomClass As New Random() Dim RandomNumber As Double

Dim holder As Double

Dim objApp As Microsoft.Office.Interop.Excel.Application 'used in accessing an manipulating an excel spreadsheet Dim objBook As Microsoft.Office.Interop.Excel._Workbook 'for excel

Private Sub Button1_Click(ByVal sender As System.Object, ByVal e As System.EventArgs) Handles Button1.Click

Dim objBooks As Microsoft.Office.Interop.Excel.Workbooks 'for excel Dim objBheets As Microsoft.Office.Interop.Excel.Sheets 'for excel Dim objBheet As Microsoft.Office.Interop.Excel.Workbaet 'for excel Dim range As Microsoft.Office.Interop.Excel.Range 'for excel

'Create a new instance of Excel and start a new workbook: objApp = New Microsoft.Office.Interop.Excel.Application() objBooks = objApp.Workbook objBooks = objBooks.Add objSheets = objShoets(1)

'range = objSheet.Range("A1", Reflection.Missing.Value) 'for excel 'range = range.Resize(Players, Rounds + 1) 'for excel

'Dim saRet(Players, Rounds + 1) As Double 'This matrix will temporarily store the match outcomes and the predictions of the nonMIs.

'range.Value = saRet 'indicates the cells of the spreadsheet that will be loaded into saRet

'Return control of Excel to the user objApp.Visible = True objApp.UserControl = True

'Clean up a little. range = Nothing objSheet = Nothing objSheets = Nothing objBooks = Nothing Randomize()

For big_loop = 1 To Big_Loop_Size

For x = 1 To Number_of_Natural_Categories
Natural_Category_Counts(x) = 0 Next

'Choose the mean values for categories For x = 1 To Number_of_Natural_Categories For y = 1 To Number_of_intensions RandomNumber = RandomClass.NextDouble() Natural_Category_Means(x, y) = RandomNum

Next Next

'Determine Number of Objects for each Category: holder = 0 For x = 1 To Number_of_Natural_Categories RandomNumber = RandomClass.NextDouble()

Natural_Category_Probabilities(x) = RandomNumber holder = holder + RandomNumber

Novt

For x = 1 To Number_of_Natural_Categories Natural_Category_Probabilities(x) = Natural_Category_Probabilities(x) / holder Novt

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'Determine the position of each object: objectcounter = \boldsymbol{\theta}
                        holder = Math.Ceiling(Number_of_Dimensions / 2) * 2
                        For x = 1 To Number of Natural Categories
                               For y = 1 To Natural_Category_Counts(x)
                                       objectcounter = objectcounter + 1
                                      GaussNumDist(0, Std Dev for Natural Categories, holder)
                                      For z = 1 To Number_of_Dimensions
                                               Object_Coordinates(objectcounter, z) = Natural_Category_Means(x, z) + GaussNumArray(z)
                                             If Object_Coordinates(objectcounter, z) > 1 Then
    Object_Coordinates(objectcounter, z) = 1
End If
    If Object_Coordinates(objectcounter, z) < 0 Then
    Object_Coordinates(objectcounter, z) = 0
End If</pre>
                              Next
                        Nevt
                              nerate a sample:

x = 1 To Sample_Size

RandomNumber = Random(Llass.NextDouble()

RandomNumber = Random(Number* Number_of_Objects

RandomNumber = Nath.Celling(RandomNumber)

For y = 1 To Number_of_Dimensions

Nersiangle_Object_Coordinates(x, y) = Object_Coordinates(RandomNumber, y)
                        'Gen
                               Next
                         Novt
                       'loop to run for different choices of initial centroids:
Total_Object_to_Assigned_Top_Centroids_Distance = 100000000
For L = 1 To 10
                               'Choose initial centroids:
For x = 1 To Number_of_Centroids
for y = 1 To Number_of_Dimensions
RandomKumber = RandomClass.NextDouble()
Provisional_Centroid_Coordinates(x, y) = RandomNumber
Newt
                               Next
Next
                               'Assign Objects to Centroids:

For a = 1 To Sample_Size

Distance_Holder2 = 10

For x = 1 To Number_of_Centroids

Distance_Holder1 = 0

For y = 1 To Number_of_Dimensions

Distance_Holder1 = Distance_Holder1 + distance(Provisional_Centroid_Coordinates(x, y), Sample_Object_Coordinates(a, y))

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                             , - 1 to Number_of_Dimensions
Distance_Holder1 = Distance_Holder1 + distanc
Next
If Distance_Holder1 < Distance_Holder2 Then
Object_Provisional_centroid_Assignent(a) = x
Distance_Holder2 = Distance_Holder1
End If
Next
'Compute Total Subclass to Assigned Centroids Distance:
Total_Object_to_Assigned_Provisional_Centroids_Distance = 0
For x = 1 To Sample_Size
If Object_Provisional_Centroid_Assignent(a) = x Then
For y = 1 To Number_of Dimensions
Total_Object_to_Assigned_Provisional_Centroids_Distance = Total_Object_to_Assigned_Provisional_Centroids_Distance + distance(Provisional_Centroid_Coordinates(x, y),
Sample_Object_Coordinates(a, y))
Next
                             رa, y
Ne.
End If
Next
Next
                                'Iterate Lloyd's Algorythm:
For r = 1 To 10
                                       'Update Centroids:
For x = 1 To Number_of_Centroids
Number_of_Objects_Attached_to_Centroid_Counter = 0
For y = 1 To Number_of_Dimensions
Updated_Centroid_Coordinates(x, y) = 0
Northing
                                                      t = 1 To Sample_Size

If Object_Provisional_Centroid_Assignent(a) = x Then

For y = 1 To Number_of Dimensions

Updated_Centroid_Coordinates(x, y) = Updated_Centroid_Coordinates(x, y) + Sample_Object_Coordinates(a, y)

Next
                                               Next
For
                                                       Next

If Nubber of Dbjetts Attached to Centroid_Counter > 0 Then

For y = T To Number of Dimensions

Updated_Centroid_Coordinates(x, y) = Updated_Centroid_Coordinates(x, y) / Number_of_Objetts_Attached_to_Centroid_Counter
                                     'Assign Objects to Centroids:
For a + ITo Sample_Size
Distance_Nolder2 = 10
For x = 1 To Number_of_Centroids
Distance_Holder1 = 0
For y = 1 To Number_of_Dimensions
For y = 1 To Number_of_Dimensions
Willstance_Holder1 = Distance_Holder1 + distance(Updated_Centroid_Coordinates(x, y), Sample_Object_Coordinates(a, y))
                                     y = 1 To Number_of_Dimensions
Distance_Holder1 = Distance_Holder1 + dit
Next
If Pistance_Holder1 < Distance_Holder2 Then
Object_Updated_Centroid_Assignent(a) = x
Distance_Holder2 = Distance_Holder1
End If
Next
Next
                                       'Compute Total Object to Assigned Centroids Distance:
Total_Object_to_Assigned_Updated_Centroids_Distance = 0
For x = 1 To Number_of_Centroids
For a = 1 To Sample_Size
If Object_Updated_Centroid_Assignent(a) = x Then
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For y = 1 To Number_of_Dimensions
Total_Object_to_Assigned_Updated_Centroids_Distance = Total_Object_to_Assigned_Updated_Centroids_Distance + distance(Updated_Centroids_Coordinates(x, y), Next End If Next Next Sample_Object_Coordinates(a, y)) 'Test whether Updated Centroids are better. If Total_Object_to_Assigned_Updated_Centroids_Distance < Total_Object_to_Assigned_Provisional_Centroids_Distance Total_Object_to_Assigned_Updated_Centroids_Distance For x = 1 To Number_of_Centroids For y = 1 To Number_of_Dimensions Provisional_Centroid_Coordinates(x, y) = Updated_Centroid_Coordinates(x, y) Next Next
Next
For a = 1 To Sample_Size
For a = 1000
Next
Else
F = 1000
End If Next Next For a 1 To Sample_Size Sample_Object_Top_Centroid_Assignment(a) = Object_Provisional_Centroid_Assignment(a) Next End If Next 'compute frequencies of fitted class membership in sample For x = 1 To Number_of_Centroids
Fitted_Class_Frequencies_in_Sample(x) = 0 Next Next For y = 1 To Number_of_centroids Fitted_Class_Frequencies_in_Sample(y) = Fitted_Class_Frequencies_in_Sample(y) / Sample_Size Next ute frequencies of fitted class membership in population 'compute frequencies of fitted class membership in population 'begin by assigning objects to centroids: For a = 1 To Number_of_Objects Distance_Holder1 = 00000 for x = 1 To Number_of_Centroids Distance_Holder1 = Distance_Holder1 + distance(Top_Centroid_Coordinates(x, y), Object_Coordinates(a, y)) How Distance_Holder1 = Distance_Holder1 + distance(Top_Centroid_Coordinates(x, y), Object_Coordinates(a, y)) For x = 1 To Number_of_Centroids
 Fitted_Class_Frequencies_in_Universe(x) = 0 End if Next Next For y = 1 To Number_of_Centroids Fitted_Class_Frequencies_in_Universe(y) = Fitted_Class_Frequencies_in_Universe(y) / Number_of_Objects Next 'Now compute the sample and population frequencies for rectanglular categories: For x=1 To Nummer_of_Centroids Num_Rectangular_Category_Frequencies_in_Sample(x) = 0 Rectangular_Category_Frequencies_en______
Next
For x = 1 To Sample_Size
For y = 1 To Sample_Size
For y = 1 To Number_of_Centroids
If (y - 1) / Number_of_Centroids
Rectangular_Category_Frequencies_in_Sample(y) = Rectangular_Category_Frequencies_in_Sample(y) + 1
End If
Next
Next
Next Next Next For x = 1 To Number_of_Centroids Rectangular_Category_Frequencies_in_Sample(x) / Sample_Size tt
tx = 1 To Number_of_Objects
For y = 1 To Number_of_Centroids
If (y - 1) / Number_of_Centroids <= Object_Coordinates(x, 1) And Object_Coordinates(x, 1) <= y / Number_of_Centroids
Then
Rectangular_Category_Frequencies_in_Universe(y) = Rectangular_Category_Frequencies_in_Universe(y) + 1
Next</pre> nex. Mext = I To Number_of_Centroids Rectangular_Category_Frequencies_in_Universe(x) = Rectangular_Category_Frequencies_in_Universe(x) / Number_of_Objects Next 'Now compute the sample and population frequencies for non-convex categories that are unions of rectangular categories: 'For x = 1 To Number_of_Centroids 'Next 'For x = 1 To Sample_Size 'For y = 1 To Number_of_Centroids + 2)) + 0.5 << Sample_Object_Coordinates(x, 1) And Sample_Object_Coordinates(x, 1) <= (y / (Number_of_Centroids * 2)) + 0.5) Or ((y - 1) / (N 'For x = 1 To Number_of_Centroids ' Non_convex_Category_Frequencies_in_Sample(x) = Non_convex_Category_Frequencies_in_Sample(x) / Sample_Size 'Next 'For x = 1 To Number_of_Centroids
' Non_convex_Category_Frequencies_in_Universe(x) = 0 ' Non_convex_fategory_Prequencies_in_universerve, '
'Next
'For x = 1 To Number_of_Objects
' For y = 1 To Number_of_centroids * 2)) + 0.5 <= Object_Coordinates(x, 1) And Object_Coordinates(x, 1) <= (y / (Number_of_Centroids * 2)) + 0.5) Or ((y - 1) / (Number_of_Centroids *
2) <= Object_Coordinates(x, 1) And Object_Coordinates(x, 1) And Object_Coordinates(x, 1) <= (y / (Number_of_Centroids * 2)) + 0.5) Or ((y - 1) / (Number_of_Centroids *
2) <= Object_Coordinates(x, 1) And Object_Coordinates(x, 1) And Object_Coordinates(x, 1) <= (y / (Number_of_Centroids * 2)) + 0.5) Or ((y - 1) / (Number_of_Centroids *
2) <= Object_Coordinates(x, 1) And Object_Coordinates(x, 1) And Object_Coordinates(x, 1) <= (y / (Number_of_Centroids * 2)) + 0.5) Or ((y - 1) / (Number_of_Centroids *
2) <= Object_Coordinates(x, 1) And Object_Coor

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'For x = 1 To Number_of_Centroids
' Non_convex_Category_Frequencies_in_Universe(x) = Non_convex_Category_Frequencies_in_Universe(x) / Number_of_Objects
                        'Next
                       For x = 1 To Number_of_Centroids
Fitted_Category_Accuracy(big_loop) + Fitted_Category_Accuracy(big_loop) + Math.Abs(Fitted_Class_Frequencies_in_Sample(x) - Fitted_Class_Frequencies_in_Universe(x))
Rectangular_Category_Accuracy(big_loop) = Rectangular_Category_Accuracy(big_loop) + Math.Abs(Rectangular_Category_Frequencies_in_Sample(x) - Rectangular_Category_Frequencies_in_Universe(x))
'Non_convex_Category_Accuracy(big_loop) = Non_convex_Category_Accuracy(big_loop) + Math.Abs(Non_convex_Category_Frequencies_in_Sample(x) - Non_convex_Category_Frequencies_in_Universe(x))
                       Fitted_Category_Accuracy(big_loop) = Fitted_Category_Accuracy(big_loop) / Number_of_Centroids
Rectangular_Category_Accuracy(big_loop) = Rectangular_Category_Accuracy(big_loop) / Number_of_Centroids
'Mon_convex_Category_Accuracy(big_loop) = Non_convex_Category_Accuracy(big_loop) / Number_of_Centroids
               Next
              Mean_Fitted_Category_Accuracy = Mean_Fitted_Category_Accuracy / Big_Loop_Size
Mean_Rectangular_Category_Accuracy = Mean_Rectangular_Category_Accuracy / Big_Loop_Size
Mean_Non_Convex_Category_Accuracy = Mean_Non_Convex_Category_Accuracy / Big_Loop_Size
                objApp.Cells(1, 1) = "Big_Loop_Size"
objApp.Cells(1, 2) = Big_Loop_Size
               objApp.Cells(2, 1) = "Number_of_Objects"
objApp.Cells(2, 2) = Number_of_Objects
               objApp.Cells(3, 1) = "Sample_Size"
objApp.Cells(3, 2) = Sample_Size
               objApp.Cells(4, 1) = "Number_of_Dimensions"
objApp.Cells(4, 2) = Number_of_Dimensions
               objApp.Cells(5, 1) = "Number_of_Natural_Categories"
objApp.Cells(5, 2) = Number_of_Natural_Categories
               objApp.Cells(6, 1) = "Std_Dev_for_Natural_Categoriese"
objApp.Cells(6, 2) = Std_Dev_for_Natural_Categories
               objApp.Cells(7, 1) = "Number_of_Centroids"
objApp.Cells(7, 2) = Number_of_Centroids
               objApp.Cells(8, 1) = "Mean Error Rate for Natural Categories"
objApp.Cells(8, 2) = Mean_Fitted_Category_Accuracy
               objApp.Cells(9, 1) = "Mean Error Rate for Non-Natural Categories"
objApp.Cells(9, 2) = Mean_Rectangular_Category_Accuracy
                'objApp.Cells(10, 1) = "Mean_Non_convex_Category_Accuracy"
'objApp.Cells(10, 2) = Mean_Non_convex_Category_Accuracy
        End Sub
       Public Function distance(ByRef r As Double, ByVal s As Double) As Double
Dim dist As Double = 0
dist = (r - s) * (r - s) 'squared
'dist = Math.Abs(r - s) 'manhatten
'If dist < 0 Or dist > 10 Then
'fd dist = dist
Return dist
End Function
End Class
Module Module1
Friend GaussNumArray() As Double
Friend intICell As Long
       ReDim GaussNumArray(SampleSize)
              Do While (intICell < (SampleSize + 1))
   Call NumDist(Mean, StdDev)
   Application.DoEvents()
</pre>
       Loop
End Function
        Sub NumDist(ByVal meanin As Double, ByVal sdin As Double)
              Defining variables
Dim dblR1 As Double
Dim dblR2 As Double
Dim taka As Double
Dim taka As Double
Dim trans As Double
Dim trans As Double
Dim dblY1 As Double
Dim Pi As Double
Pi = 4 * Atan(1)
               'Get two random numbers
dblR1 = (2 * UniformRandomNumber()) - 1
dblR2 = (2 * UniformRandomNumber()) - 1
               circ = (dblR1 ^ 2) + (dblR2 ^ 2)
                                                                                        'Radius of circle
               If circ >= 1 Then 'If outside unit circle, then reject number
Call NumDist(meanin, sdin)
Exit Sub
End If
               'Transform to Gaussian
trans = Sqrt(-2 * Log(circ) / circ)
               dblY1 = (trans * dblR1 * sdin) + meanin
dblY2 = (trans * dblR2 * sdin) + meanin
               GaussNumArray(intICell) = dblY1 'First number
               'Increase intICell for next random number
intICell = (intICell + 1)
               GaussNumArrav(intICell) = dblY2 'Second number
               'Increase intICell again ready for next call of ConvertNumberDistribution intICell = (intICell + 1) \,
       End Sub
        Friend Function UniformRandomNumber() As Double
               'Defining constants
Const IM1 As Double = 2147483563
Const IM2 As Double = 2147483399
Const AM As Double = (1.0# / IM1)
Const IMM1 As Double = (IM1 - 1.0#)
Const IA1 As Double = 40014
Const IA2 As Double = 40692
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Const IQ1 As Double = 53668
Const IQ2 As Double = 1221
Const IR2 As Double = 1221
Const MD1/AB As Double = 120
Const MD1/AB As Double = (100000012
Const MD1/AB As Double = (100000012
Const MD1/AB As Double = (100000012
Const MD1/AB As Double
Dis Jata S Double = (100000012
Const MD1/AB S Double
Static id was Double
Const inversion
Static id was Double
If (dd was Double
If (dd was Double
If (dd was Double
Static id was Dou
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